

2018-2019 Guide

December 3rd- February 8th

<u>Eureka</u>

Module 3: Comparison of Length, Weight, Capacity, and Numbers to 10



ORANGE PUBLIC SCHOOLS OFFICE OF CURRICULUM AND INSTRUCTION OFFICE OF MATHEMATICS

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Module 3 Performance Overview

- In Topic A and B, students on comparisons of length using terminology such as "longer than", "shorter than" and "as long as"
- Topic C focuses on comparison of weight, and Topic D on comparison of volume. Each of these topics opens with an identification of the attribute being compared within the natural context of the lesson
- Topic E begins with an analysis using the question, "Are there enough?" This leads naturally from exploring when and if there is enough space to seeing whether there are enough chairs for a small set of students?"
- Topic E bridges into Topics F and G, which present a sequence building toward the comparison of numerals. Topic F begins with counting and matching sets to compare.
- The module culminates in a three-day exploration, one day devoted to each attribute: length, weight, and volume The module closes with a culminating task devoted to distinguishing between the measurable attributes of a set of objects: a water bottle, cup, dropper, and juice box.



<u>Module 3: Comparison of Length, Weight, Capacity and Numbers to 10</u> <u>Pacing:</u> December 3 rd - February 8 th <u>38 Days</u>						
Topic Lesson Lesson Objective/ Supportive Videos						
Topic A:	Lesson 1	Compare lengths using taller than and shorter than with aligned and non-aligned endpoints.				
Comparison of Length and Weight	Lesson 2	Compare length measurements with string.				
weight	Lesson 3	Make a series of longer than and shorter than compari- sons.				
Topic B:	Lesson 4	Compare the length of linking cube sticks to a 5-stick.				
Comparison of Length and	Lesson 5	Determine which linking cube stick is longer than or shorter than the other.				
Height of Linking Cube Sticks Within 10	Lesson 6	Compare the length of linking cube sticks to various objects				
	Lesson 8	Compare using heavier than and lighter than with classroom objects				
Topic C: Comparison of	Lesson 9	Compare objects using heavier than, lighter than, and the same as with balance scales				
Weight	Lesson 10	Compare the weight of an object to a set of unit weights on a balance scale				
	Lesson 11	Observe conservation of weight on the balance scale.				
	Lesson 12	Compare the weight of an object with sets of different objects on a balance scale				
Topic D:	Lesson 13	Compare volume using more than, less than, and the same as by pouring.				
Comparison of Volume	Lesson 14	Explore conservation of volume by pouring				

	Lesson 15	Compare using the same as with units			
		Mid-Module Assessment Task			
		(Interview Style)			
		January 3 rd -7 th 2019			
	Lesson 17	Compare to find if there are enough			
Topic E: Are there	Lesson 18	Compare using more than and the same as.			
Enough?	Lesson 19	Compare using fewer than and the same as.			
	Lesson 20	Relate more and less to length.			
Topic F: Comparison of	Lesson 21	Compare sets informally using more, less, and fewer.			
Sets Within 10	Lesson 22	Identify and create a set that has the same number of objects			
	Lesson 23	Reason to identify and make a set that has 1 more			
	Lesson 24	Reason to identify and make a set that has 1 less			
Topic G:	Lesson 25	Match and count to compare a number of objects. State which quantity is more.			
Comparison of Numerals &	Lesson 26	Match and count to compare two sets of objects. State which quantity is less			
Topic H: Clarification of Measurable	Lesson 27	Strategize to compare two sets			
Attributes	Lesson 28	Visualize quantities to compare two numerals.			
	Lesson 32	Culminating task—describe measurable attributes of single objects.			
End-of- Module Assessment Task (Interview Style: 3 days) February 6-8 th 2019					

NJSLS Standards

Module 3: Comparison of Length, Weight, Capacity and Numbers to 10				
KCC.6	Identify whether the number of objects in one group is greater than, less than, or equal to the numb of objects in another group e.g by us- ing matching and counting strategies			
Include gro	oups with up to ten objects.			
Know num	ber names and the count sequence			
 Students use their counting ability to compare sets of objects). They may use matching strategies, counting strategies or equal shares to determine whether one group is greater than, less than, or equal to the number of objects in anothe group. Example: I lined up one square and one triangle. Since there is one extra triangle, there are more triangles than squares. (Matching Strategy) Example : I counted the squares and I got 4. Then I counted the triangles and g 5. Since 5 is bigger than 4, there are more triangles than squares. (Counting Strategy) Example: I put them in a pile. I then took away objects. Every time I took a square, I also took a triangle. When I had taken almost all of the shapes away, there was still a triangle left. That means that there are more triangles than squares. (Equal Shares) 				
K.CC.7 Compare two numbers between 1 and 10 presented as written als				

•	It is important for students to have multiple hands on opportunities to match, re-
	arrange, and count sets of objects to address misunderstanding

- Utilize open-ended questions which will develop reason and mathematical arguments called for in Standards for Mathematical Practice
- Know number names and the count sequence
- Students need multiple experiences with actual sets of objects to develop a strong conceptual understanding of "how much/how many" certain numbers represent using concrete materials before they compare using only more abstract representations such as pictorial or numerals

K.MD.A.1

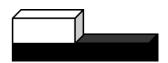
Describe measurable attributes of objects, such as length or weight. Describe several measurable attributes of a single object

- Provide learning opportunities for students to identify and describe different measurable attributes of objects, such as height and weight.
 Example: Teachers develop vocabulary by asking "How is it more?" or "How is it bigger?"
- Allow children to measure a variety of things they find in the classroom with nonstandard measurement tools such as string.
- Model measurement vocabulary **Example:** "We discovered the length of our desks is 6 strong *long*

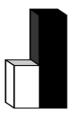
K.MD.A.2	Directly compare two objects with a measurable attribute in common to see which object has "more" or less of" the attribute, and describe the dif- ference. For example, directly compare the heights of two children and describe one child as taller/shorter
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- Provide numerous experiences for students to directly compare two objects.
- Ensure students are matching ends of objects to get accurate measurement comparison. Provide ample experiences with comparing objects in order to discover the importance of lining up the ends of objects in order to have an accurate measurement.
- Direct comparisons are made when objects are put next to each other, such as two children, two books, two pencils.
 Example: a student may line up two blocks and say, "The blue block is a lot longer than the white one."

Students are not comparing objects that cannot be moved and lined up next to each other.



Once students develop the conservation of length, they realize that a block's length remains constant when it is placed in different orientations.
 Example: The dark block is always longer than the lighter block



M : Major Content

S: Supporting Content

A : Additional Content

DerminologyBalance scale (tool for weight measurement) Capacity (with reference to volume) Compare (specifically using direct comparison) Endpoint (with reference to alignment for direct comparison) Enough/not enough (comparative term) Heavier than/lighter than (weight comparison) Height (vertical distance measurement from bottom to top) Length (distance measurement from end to end; in a rectangular shape, length can be used to describe any of the four sides) Longer than/shorter than (length comparison)

- More than/fewer than (discrete quantity comparison)
- More than/less than (volume, area, and number comparisons)
- Taller than/shorter than (height comparison)
- The same as (comparative term)
- Weight (heaviness measurement)

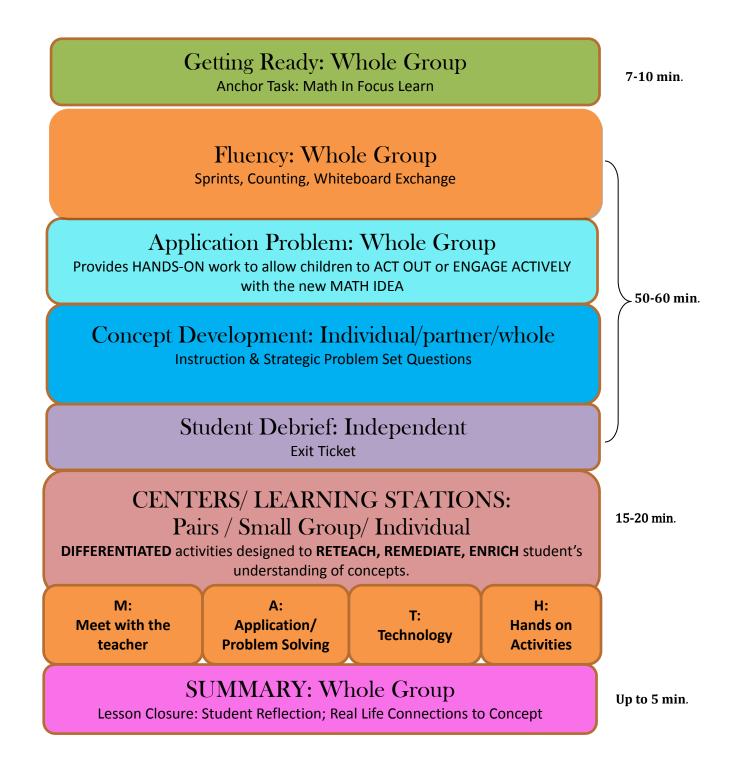
Teaching Representations/ Manipulatives/ Tools:

- Balance scales
- Centimeter cubes
- clay
- linking cubes in sticks with a color change at five
- Plastic cups and containers for measuring volume



Module 3 Assessment / Authentic Assessment Recommended Framework								
Assessment	CCSS	Estimated Time	Format					
	<u>Eureka Math</u>							
<u>Module 3: Compo</u>	<mark>rison of Length, We</mark>	ight, Capacity	, and					
	<u>Numbers to 10</u>							
Optional Mid-Module As- sessment (Interview Style)	K.MD.1 K.MD.2	1 Block	Individual or Small Group with Teacher					
Optional End of Module Assessment (Interview Style)	K.CC.6 K.CC.7 K.MD.1 K.MD.2	1 Block	Individual or Small Group with Teacher					

Kindergarten Ideal Math Block



Eureka Lesson Structure:

Fluency:

- Sprints
- Counting : Can start at numbers other than 0 or 1 and might include supportive concrete material or visual models
- Whiteboard Exchange

Application Problem:

- Engage students in using the RDW Process
- Sequence problems from simple to complex and adjust based on students' responses
- Facilitate share and critique of various explanations, representations, and/or examples.

Concept Development: (largest chunk of time)

Instruction:

- Maintain overall alignment with the objectives and suggested pacing and structure.
- Use of tools, precise mathematical language, and/or models
- Balance teacher talk with opportunities for peer share and/or collaboration
- Generate next steps by watching and listening for understanding

Problem Set: (Individual, partner, or group)

- Allow for independent practice and productive struggle
- Assign problems strategically to differentiate practice as needed
- Create and assign remedial sequences as needed

Student Debrief:

- Elicit students thinking, prompt reflection, and promote metacognition through student centered discussion
- Culminate with students' verbal articulation of their learning for the day
- Close with completion of the daily Exit Ticket (opportunity for informal assessment that guides effective preparation of subsequent lessons) as needed.

Number Talks Cheat Sheet

What does Number Talks look like?

- Students are near each other so they can communicate with each other (central meeting place)
- Students are mentally solving problems
- Students are given thinking time
- Thumbs up show when they are ready
- Teacher is recording students' thinking

Communication

- Having to talk out loud about a problem helps students clarify their own thinking
- Allow students to listen to other's strategies and value other's thinking
- Gives the teacher the opportunity to hear student's thinking

Mental Math

- When you are solving a problem mentally you must rely on what you know and understand about the numbers instead of memorized procedures
- You must be efficient when computing mentally because you can hold a lot of quantities in your head

Thumbs Up

- This is just a signal to let you know that you have given your students enough time to think about the problem
- If will give you a picture of who is able to compute mentally and who is struggling
- It isn't as distracting as a waving hand

Teacher as Recorder

- Allows you to record students' thinking in the correct notation
- Provides a visual to look at and refer back to
- Allows you to keep a record of the problems posed and which students offered specific strategies

Purposeful Problems

- Start with small numbers so the students can learn to focus on the strategies instead of getting lost in the numbers
- Use a number string (a string of problems that are related to and scaffold each other)

Starting Number Talks in your Classroom

- Start with specific problems in mind
- Be prepared to offer a strategy from a previous student
- It is ok to put a student's strategy on the backburner
- Limit your number talks to about 15 minutes
- Ask a question, don't tell!

The teacher asks questions:

- Who would like to share their thinking?
- Who did it another way?
- How many people solved it the same way as Billy?
- Does anyone have any questions for Billy?
- Billy, can you tell us where you got that 5?
- How did you figure that out?

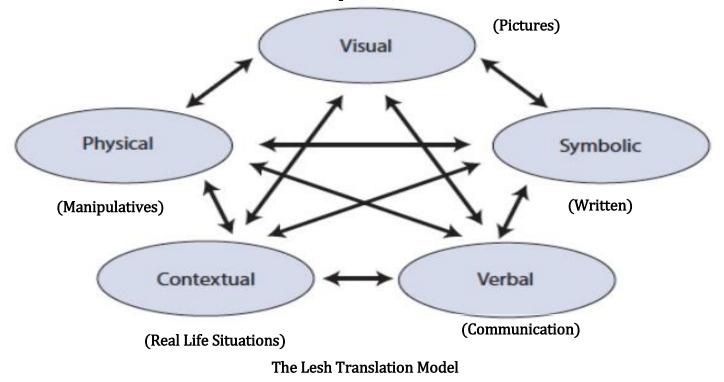
Student	Name: _
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Task:		

School: _____ Teacher: _____ Date:

	STUDENT FRIENDLY RUBRIC				SCORE
"I CAN"	a start 1	getting there 2	that's it 3	WOW! 4	SCORE
Understand	Understand I need help.		I do not need help.	I can help a class- mate.	
Solve	I am unable to use a strategy.	I can start to use a strategy.	I can solve it more than one way.	I can use more than one strategy and talk about how they get to the same answer.	
Say or Write	I am unable to say or write.	I can write or say some of what I did.	I can write and talk about what I did. I can write or talk about why I did it.	I can write and say what I did and why I did it.	
Draw or Show	I am not able to draw or show my thinking.	I can draw, but not show my thinking; or I can show but not draw my thinking;	I can draw and show my thinking	I can draw, show and talk about my think- ing.	

Use and Connection of Mathematical Representations



Each oval in the model corresponds to one way to represent a mathematical idea.

Visual: When children draw pictures, the teacher can learn more about what they understand about a particular mathematical idea and can use the different pictures that children create to provoke a discussion about mathematical ideas. Constructing their own pictures can be a powerful learning experience for children because they must consider several aspects of mathematical ideas that are often assumed when pictures are pre-drawn for students.

Physical: The manipulatives representation refers to the unifix cubes, base-ten blocks, fraction circles, and the like, that a child might use to solve a problem. Because children can physically manipulate these objects, when used appropriately, they provide opportunities to compare relative sizes of objects, to identify patterns, as well as to put together representations of numbers in multiple ways.

Verbal: Traditionally, teachers often used the spoken language of mathematics but rarely gave students opportunities to grapple with it. Yet, when students do have opportunities to express their mathematical reasoning aloud, they may be able to make explicit some knowledge that was previously implicit for them.

Symbolic: Written symbols refer to both the mathematical symbols and the written words that are associated with them. For students, written symbols tend to be more abstract than the other representations. I tend to introduce symbols after students have had opportunities to make connections among the other representations, so that the students have multiple ways to connect the symbols to mathematical ideas, thus increasing the likelihood that the symbols will be comprehensible to students.

Contextual: A relevant situation can be any context that involves appropriate mathematical ideas and holds interest for children; it is often, but not necessarily, connected to a real-life situation.

The Lesh Translation Model: Importance of Connections

As important as the ovals are in this model, another feature of the model is even more important than the representations themselves: The arrows! The arrows are important because they represent the connections students make between the representations. When students make these connections, they may be better able to access information about a mathematical idea, because they have multiple ways to represent it and, thus, many points of access.

Individuals enhance or modify their knowledge by building on what they already know, so the greater the number of representations with which students have opportunities to engage, the more likely the teacher is to tap into a student's prior knowledge. This "tapping in" can then be used to connect students' experiences to those representations that are more abstract in nature (such as written symbols). Not all students have the same set of prior experiences and knowledge. Teachers can introduce multiple representations in a meaningful way so that students' opportunities to grapple with mathematical ideas are greater than if their teachers used only one or two representations.

Concrete Pictorial Abstract (CPA) Instructional Approach

The CPA approach suggests that there are three steps necessary for pupils to develop understanding of a mathematical concept.

Concrete: "Doing Stage": Physical manipulation of objects to solve math problems. **Pictorial:** "Seeing Stage": Use of imaged to represent objects when solving math problems.

Abstract: "Symbolic Stage": Use of only numbers and symbols to solve math problems.

CPA is a gradual systematic approach. Each stage builds on to the previous stage. Reinforcement of concepts are achieved by going back and forth between these representations and making connections between stages. Students will benefit from seeing parallel samples of each stage and how they transition from one to another.

Read, Draw, Write Process

READ the problem. Read it over and over.... And then read it again.

DRAW a picture that represents the information given. During this step students ask themselves: Can I draw something from this information? What can I draw? What is the best model to show the information? What conclusions can I make from the drawing?WRITE your conclusions based on the drawings. This can be in the form of a number sentence, an equation, or a statement.

Students are able to draw a model of what they are reading to help them understand the problem. Drawing a model helps students see which operation or operations are needed, what patterns might arise, and which models work and do not work. Students must dive deeper into the problem by drawing models and determining which models are appropriate for the situation.

While students are employing the RDW process they are using several Standards for Mathematical Practice and in some cases, all of them.

Mathematical Discourse and Strategic Questioning

Discourse involves asking strategic questions that elicit from students their understanding of the context and actions taking place in a problem, how a problem is solved and why a particular method was chosen. Students learn to critique their own and others' ideas and seek out efficient mathematical solutions.

While classroom discussions are nothing new, the theory behind classroom discourse stems from constructivist views of learning where knowledge is created internally through interaction with the environment. It also fits in with socio-cultural views on learning where students working together are able to reach new understandings that could not be achieved if they were working alone.

Underlying the use of discourse in the mathematics classroom is the idea that mathematics is primarily about reasoning not memorization. Mathematics is not about remembering and applying a set of procedures but about developing understanding and explaining the processes used to arrive at solutions.

Teacher Questioning:

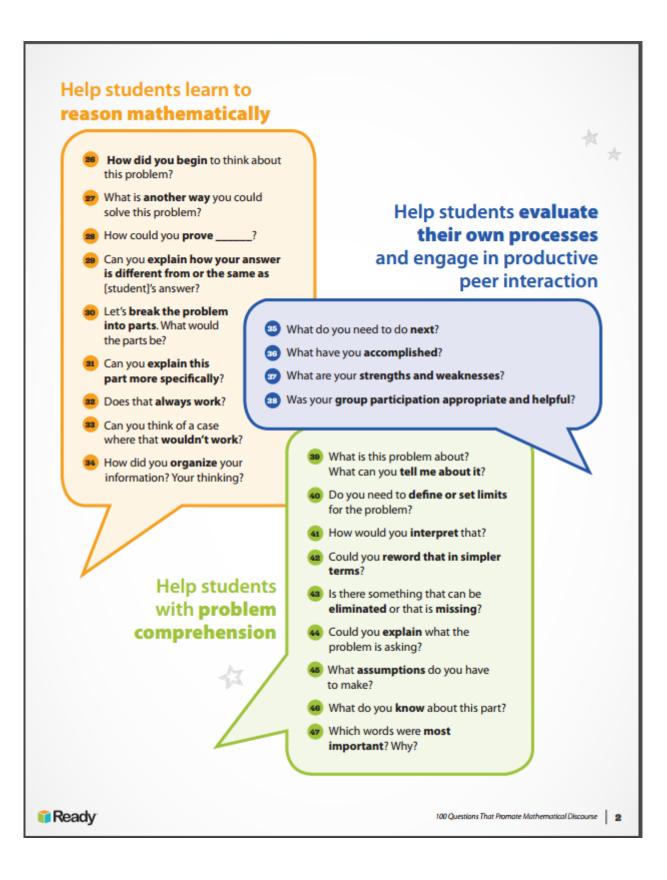
Asking better questions can open new doors for students, promoting mathematical thinking and classroom discourse. Can the questions you're asking in the mathematics classroom be answered with a simple "yes" or "no," or do they invite students to deepen their understanding?



Albert Einstein

To help you encourage deeper discussions, here are 100 questions to incorporate into your instruction by Dr. Gladis Kersaint, mathematics expert and advisor for Ready Mathematics.

Disco	ematical
 What strategy did you use? Do you agree? Do you disagree? Would you ask the rest of the class that question? Could you share your method with the class? What part of what he said do you understand? Would someone like to share? Can you convince the rest of us the your answer makes sense? What do others think about what [student] said? 	 Have you discussed this with your group? With others? Did anyone get a different answer? Where would you go for help? Did everybody get a fair chance to talk, use the manipulatives, or be the recorder? How could you help another student without telling them the answer?
Help students rely more on themselves to determine whether something is mathematically correct	 Is this a reasonable answer? Does that make sense? Why do you think that? Why is that true? Can you draw a picture or make a model to show that? How did you reach that conclusion? Does anyone want to revise his or her answer? How were you sure your answer was right?



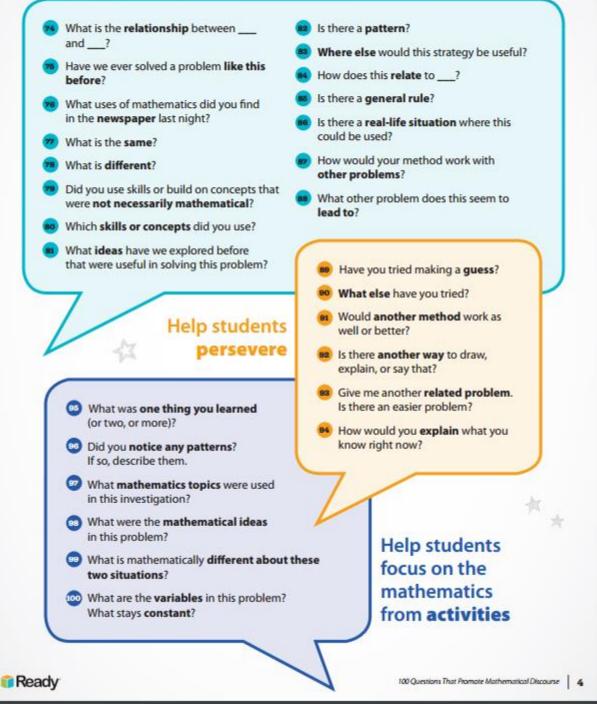
Help students learn to conjecture, invent, and solve problems

1				
	43	What would happen if?	60	How would you draw a diagram or
	40	Do you see a pattern ?	_	make a sketch to solve the problem?
	60	What are some possibilities here?	61	Is there another possible answer ? If so, explain.
	61	Where could you find the information you need?	62	Is there another way to solve the problem?
	62	How would you check your steps or your answer?	63	Is there another model you could use to solve the problem?
	63	What did not work?	60	Is there anything you've overlooked ?
	60	How is your solution method the same	65	How did you think about the problem?
	Ţ	as or different from [student]'s method?	66	What was your estimate or prediction?
	65	Other than retracing your steps, how	67	How confident are you in your answer?
		can you determine if your answers are appropriate?	68	What else would you like to know?
	66	How did you organize the information? Do you have a record ?	🔊 Ist	What do you think comes next?
				Is the solution reasonable , considering
	0	How could you solve this using tables , lists, pictures, diagrams, etc.?	•	the context?
	0	What have you tried? What steps did	0	Did you have a system ? Explain it.
	-	you take?	6	Did you have a strategy ? Explain it.
	69	How would it look if you used this model or these materials?	73	Did you have a design ? Explain it.
				* *

🗊 Ready

100 Questions That Promote Mathematical Discourse 3





Conceptual Understanding

Students demonstrate conceptual understanding in mathematics when they provide evidence that they can:

- recognize, label, and generate examples of concepts;
- use and interrelate models, diagrams, manipulatives, and varied representations of concepts;
- identify and apply principles; know and apply facts and definitions;
- compare, contrast, and integrate related concepts and principles; and
- recognize, interpret, and apply the signs, symbols, and terms used to represent concepts.

Conceptual understanding reflects a student's ability to reason in settings involving the careful application of concept definitions, relations, or representations of either.

Procedural Fluency

Procedural fluency is the ability to:

- apply procedures accurately, efficiently, and flexibly;
- to transfer procedures to different problems and contexts;
- to build or modify procedures from other procedures; and
- to recognize when one strategy or procedure is more appropriate to apply than another.

Procedural fluency is more than memorizing facts or procedures, and it is more than understanding and being able to use one procedure for a given situation. Procedural fluency builds on a foundation of conceptual understanding, strategic reasoning, and problem solving (NGA Center & CCSSO, 2010; NCTM, 2000, 2014). Research suggests that once students have memorized and practiced procedures that they do not understand, they have less motivation to understand their meaning or the reasoning behind them (Hiebert, 1999). Therefore, the development of students' conceptual understanding of procedures should precede and coincide with instruction on procedures.

Math Fact Fluency: Automaticity

Students who possess math fact fluency can recall math facts with automaticity. Automaticity is the ability to do things without occupying the <u>mind</u> with the low-level details required, allowing it to become an automatic response pattern or <u>habit</u>. It is usually the result of <u>learning</u>, <u>repetition</u>, and practice.

K-2 Math Fact Fluency Expectation

K.OA.5 Add and Subtract within 5. **1.OA.6** Add and Subtract within 10.

2.OA.2 Add and Subtract within 20.

Math Fact Fluency: Fluent Use of Mathematical Strategies

First and second grade students are expected to solve addition and subtraction facts using a variety of strategies fluently.

1.0A.6 Add and subtract within 20, demonstrating fluency for addition and subtraction within 10.

Use strategies such as:

- counting on; making ten (e.g., 8 + 6 = 8 + 2 + 4 = 10 + 4 = 14);
- decomposing a number leading to a ten (e.g., 13 4 = 13 3 1 = 10 1 = 9);
- using the relationship between addition and subtraction; and
- creating equivalent but easier or known sums.

2.NBT.7 Add and subtract within 1000, using concrete models or drawings and strategies based on:

- \circ place value,
- \circ properties of operations, and/or
- \circ $\,$ the relationship between addition and subtraction;

Evidence of Student Thinking

Effective classroom instruction and more importantly, improving student performance, can be accomplished when educators know how to elicit evidence of students' understanding on a daily basis. Informal and formal methods of collecting evidence of student understanding enable educators to make positive instructional changes. An educators' ability to understand the processes that students use helps them to adapt instruction allowing for student exposure to a multitude of instructional approaches, resulting in higher achievement. By highlighting student thinking and misconceptions, and eliciting information from more students, all teachers can collect more representative evidence and can therefore better plan instruction based on the current understanding of the entire class.

Mathematical Proficiency

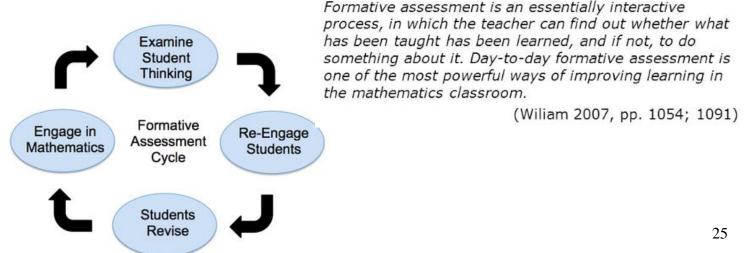
To be mathematically proficient, a student must have:

- <u>Conceptual understanding</u>: comprehension of mathematical concepts, operations, and relations;
- <u>Procedural fluency</u>: skill in carrying out procedures flexibly, accurately, efficiently, and appropriately;
- <u>Strategic competence</u>: ability to formulate, represent, and solve mathematical problems;
- <u>Adaptive reasoning</u>: capacity for logical thought, reflection, explanation, and justification;
- <u>Productive disposition</u>: habitual inclination to see mathematics as sensible, useful,

and worthwhile, coupled with a belief in diligence and one's own efficacy.

Evidence should:

- Provide a window in student thinking;
- Help teachers to determine the extent to which students are reaching the math learning goals; and
- Be used to make instructional decisions during the lesson and to prepare for subsequent lessons.



Connections to the Mathematical Practices

Student Friendly Connections to the Mathematical Practices

- 1. I can solve problems without giving up.
- 2. I can think about numbers in many ways.
- 3. I can explain my thinking and try to understand others.
- 4. I can show my work in many ways.
- 5. I can use math tools and tell why I choose them.
- 6. I can work carefully and check my work.
- 7. I can use what I know to solve new problems.
- 8. I can discover and use short cuts.

 The Standards for Mathematical Practice describe varieties of expertise that mathematics educators at all levels should seek to develop in their students.

 Image: Make sense of problems and persevere in solving them

 Image: Ima

2 Reason abstractly and quantitatively

Mathematically proficient students in Kindergarten make sense of quantities and the relationships while solving tasks. This involves two processesdecontextualizing and contextualizing.

In Kindergarten, students represent situations by decontextualizing tasks into numbers and symbols. For example, in the task, "There are 7 children on the playground and some children go line up. If there are 4 children still playing, how many children lined up?" Kindergarten students are expected to translate that situation into the equation: 7-4 =___, and then solve the task.

Students also contextualize situations during the problem solving process. For example, while solving the task above, students refer to the context of the task to determine that they need to subtract 4 since the number of children on the playground is the total number of students except for the 4 that are still playing. Abstract reasoning also occurs when students measure and compare the lengths of objects.

Construct viable arguments and critique the reasoning of others

Mathematically proficient students in Kindergarten accurately use mathematical terms to construct arguments and engage in discussions about problem solving strategies. For example, while solving the task, "There are 8 books on the shelf. If you take some books off the shelf and there are now 3 left, how many books did you take off the shelf?" students will solve the task, and then be able to construct an accurate argument about why they subtracted 3 form 8 rather than adding 8 and 3. Further, Kindergarten students are expected to examine a variety of problem solving strategies and begin to recognize the reasonableness of them, as well as similarities and differences among them.

Model with mathematics

3

4 Mathematically proficient students in Kindergarten model real-life mathematical situations with a number sentence or an equation, and check to make sure that their equation accurately matches the problem context.

Kindergarten students rely on concrete manipulatives and pictorial representations while solving tasks, but the expectation is that they will also write an equation to model problem situations.

For example, while solving the task "there are 7 bananas on the counter. If you eat 3 bananas, how many are left?" Kindergarten students are expected to write the equation 7-3 = 4.

Likewise, Kindergarten students are expected to create an appropriate problem situation from an equation.

For example, students are expected to orally tell a story problem for the equation 4+5 = 9.

Use appropriate tools strategically

Mathematically proficient students in Kindergarten have access to and use tools appropriately. These tools may include counters, place value (base ten) blocks, hundreds number boards, number lines, and concrete geometric shapes (e.g., pattern blocks, 3-d solids). Students should also have experiences with educational technologies, such as calculators, virtual manipulatives, and mathematical games that support conceptual understand-ing.

5

During classroom instruction, students should have access to various mathematical tools as well as paper, and determine which tools are the most appropriate to use. For example, while solving the task "There are 4 dogs in the park. If 3 more dogs show up, how many dogs are they?"

Kindergarten students are expected to explain why they used specific mathematical tools."

Attend to precision

6 Mathematically proficient students in Kindergarten are precise in their communication, calculations, and measurements. In all mathematical tasks, students in Kindergarten describe their actions and strategies clearly, using grade-level appropriate vocabulary accurately as well as giving precise explanations and reasoning regarding their process of finding solutions.

For example, while measuring objects iteratively (repetitively), students check to make sure that there are no gaps or overlaps. During tasks involv-

ing number sense, students check their work to ensure the accuracy and reasonableness of solutions.

Look for and make use of structure

Mathematically proficient students in Kindergarten carefully look for patterns and structures in the number system and other areas of mathematics. While solving addition problems, students begin to recognize the commutative property, in that 1+4 = 5, and 4+1 = 5.

7 While decomposing teen numbers, students realize that every number between 11 and 19, can be decomposed into 10 and some leftovers, such as 12 = 10+2, 13 = 10+3, etc.

Further, Kindergarten students make use of structures of mathematical tasks when they begin to work with subtraction as missing addend problems, such as 5 - 1 = 2 can be written as 1 + 2 = 5 and can be thought of as how much more do I need to add to 1 to get to 5?

Look for and express regularity in repeated reasoning

Mathematically proficient students in Kindergarten begin to look for regularity in problem structures when solving mathematical tasks.

Likewise, students begin composing and decomposing numbers in different ways.

8 For example, in the task "There are 8 crayons in the box. Some are red and some are blue. How many of each could there be?"

Kindergarten students are expected to realize that the 8 crayons could include 4 of each color (4+4=8), 5 of one color and 3 of another (5+3=8), etc.

For each solution, students repeated engage in the process of finding two numbers that can be joined to equal 8.

Effective Mathematics Teaching Practices

Establish mathematics goals to focus learning. Effective teaching of mathematics establishes clear goals for the mathematics that students are learning, situates goals within learning progressions, and uses the goals to guide instructional decisions.

Implement tasks that promote reasoning and problem solving. Effective teaching of mathematics engages students in solving and discussing tasks that promote mathematical reasoning and problem solving and allow multiple entry points and varied solution strategies.

Use and connect mathematical representations. Effective teaching of mathematics engages students in making connections among mathematical representations to deepen understanding of mathematics concepts and procedures and as tools for problem solving.

Facilitate meaningful mathematical discourse. Effective teaching of mathematics facilitates discourse among students to build shared understanding of mathematical ideas by analyzing and comparing student approaches and arguments.

Pose purposeful questions. Effective teaching of mathematics uses purposeful questions to assess and advance students' reasoning and sense making about important mathematical ideas and relationships.

Build procedural fluency from conceptual understanding. Effective teaching of mathematics builds fluency with procedures on a foundation of conceptual understanding so that students, over time, become skillful in using procedures flexibly as they solve contextual and mathematical problems.

Support productive struggle in learning mathematics. Effective teaching of mathematics consistently provides students, individually and collectively, with opportunities and supports to engage in productive struggle as they grapple with mathematical ideas and relationships.

Elicit and use evidence of student thinking. Effective teaching of mathematics uses evidence of student thinking to assess progress toward mathematical understanding and to adjust instruction continually in ways that support and extend learning.

5 Practices for Orchestrating Productive Mathematics Discussions			
Practice	Description/ Questions		
1. Anticipating	What strategies are students likely to use to approach or solve a challenging high-level mathematical task?		
	How do you respond to the work that students are likely to produce?		
	Which strategies from student work will be most useful in addressing the mathematical goals?		
2. Monitoring	Paying attention to what and how students are thinking during the lesson.		
	Students working in pairs or groups		
	Listening to and making note of what students are discussing and the strategies they are using		
	Asking students questions that will help them stay on track or help them think more dee about the task. (Promote productive struggle)		
3. Selecting	This is the process of deciding the <i>what</i> and the <i>who</i> to focus on during the discussion.		
	Selection of children is guided by the mathematical goal for the lesson		
4. Sequencing	What order will the solutions be shared with the class?		
	Sequence depends largely on the teacher's goals for a lesson		
	Maximizing the chances that math goals will be achieved		
5. Connecting	Asking the questions that will make the mathematics explicit and understandable.		
	Focus must be on mathematical meaning and relationships; making links between mathematical ideas and representations.		

MATH CENTERS/ WORKSTATIONS

Math workstations allow students to engage in authentic and meaningful hands-on learning. They often last for several weeks, giving students time to reinforce or extend their prior instruction. Before students have an opportunity to use the materials in a station, introduce them to the whole class, several times. Once they have an understanding of the concept, the materials are then added to the work stations.

Station Organization and Management Sample

Teacher A has 12 containers labeled 1 to 12. The numbers correspond to the numbers on the rotation chart. She pairs students who can work well together, who have similar skills, and who need more practice on the same concepts or skills. Each day during math work stations, students use the center chart to see which box they will be using and who their partner will be. Everything they need for their station will be in their box. **Each station is differentiated**. If students need more practice and experience working on numbers 0 to 10, those will be the only numbers in their box. If they are ready to move on into the teens, then she will place higher number activities into the box for them to work with.



In the beginning there is a lot of prepping involved in gathering, creating, and organizing the work stations. However, once all of the initial work is complete, the stations are easy to manage. Many of her stations stay in rotation for three or four weeks to give students ample opportunity to master the skills and concepts.

Read *Math Work Stations* by Debbie Diller.

In her book, she leads you step-by-step through the process of implementing work stations.

MATH WORKSTATION INFORMATION CARD

Iath Workstation:	 Time:
JSLS.:	
ojective(s): By the end of this task, I will be able to:	
•	
•	
sk(s):	
•	
•	
•	
it Ticket:	
•	
•	

MATH WORKSTATION SCHEDULE				Week of:		
DAY	Technology	Problem Solving Lab	Fluency	Math	Small Group Instruc-	
	Lab		Lab	Journal	tion	
Mon.						
	Group	Group	Group	Group	BASED	
Tues.					ON CURRENT	
	Group	Group	Group	Group	OBSERVATIONAL	
Wed.					DATA	
	Group	Group	Group	Group		
Thurs.						
	Group	Group	Group	Group		
Fri.						
	Group	Group	Group	Group		

INSTRUCTIONAL GROUPING

	GROUP A		GROUP B
1		1	
2		2	
3		3	
4		4	
5		5	
6		6	
		•	
	GROUP C		GROUP D
1		1	
2		2	
3		3	
4		4	
5		5	
6		6	

Got It		Not There Yet			
Evidence shows that the student essentially has the target con-		Student shows evidence of a major misunderstanding, incorrect concepts or procedure, or a fail-			
cept or big math idea.		ure to engage in the task.			
PLD Level 5: 100% PLD Level 4: 89% PLD Level 3: 79%		PLD Level 2: 69%	PLD Level 1: 59%		
Distinguished command	Strong Command	Moderate Command	Partial Command	Little Command	
Student work shows distin-	Student work shows strong	Student work shows moderate	Student work shows partial	Student work shows little un-	
guished levels of understand-	levels of understanding of the	levels of understanding of the	understanding of the mathe-	derstanding of the mathemat-	
ing of the mathematics.	mathematics.	mathematics.	matics.	ics.	
Student constructs and com -	Student constructs and com -	Student constructs and com -	Student constructs and com-	Student attempts to constructs	
municates a complete re- sponse based on explana-	municates a complete re- sponse based on explana-	municates a complete response based on explana-	municates an incomplete re- sponse based on student's at-	and communicates a response using the:	
tions/reasoning using the:	tions/reasoning using the:	tions/reasoning using the:	tempts of explanations/ rea-	 Tools: 	
 Tools: 	 Tools: 	 Tools: 	soning using the:	• Manipulatives	
• Manipulatives	• Manipulatives	• Manipulatives	 Tools: 	• Five Frame	
• Five Frame	• Five Frame	• Five Frame	• Manipulatives	• Ten Frame	
 Ten Frame 	 Ten Frame 	 Ten Frame 	• Five Frame	• Number Line	
 Number Line 	 Number Line 	 Number Line 	 Ten Frame 	 Part-Part-Whole 	
 Part-Part-Whole 	 Part-Part-Whole 	 Part-Part-Whole 	 Number Line 	Model	
Model	Model	Model	 Part-Part-Whole 	Strategies:	
Strategies:	Strategies:	Strategies:	Model	 Drawings 	
• Drawings	• Drawings	 Drawings 	Strategies:	 Counting All 	
• Counting All	• Counting All	• Counting All	• Drawings	• Count On/Back	
• Count On/Back	• Count On/Back	• Count On/Back	• Counting All	• Skip Counting	
• Skip Counting	 Skip Counting Making Ten 	 Skip Counting Making Tan 	• Count On/Back	• Making Ten	
 Making Ten Decomposing 	 Making Ten Decomposing 	 Making Ten Decomposing 	 Skip Counting Making Ten 	 Decomposing Number 	
Number	Number	Number	• Decomposing	Precise use of math vo-	
Precise use of math vo-	Precise use of math vo-	Precise use of math vo-	Number	cabulary	
cabulary	cabulary	cabulary	Precise use of math vo-	cubulury	
Response includes an efficient			cabulary	Response includes limited evi-	
and logical progression of	Response includes a logical	Response includes a logical but	5	dence of the progression of	
mathematical reasoning and	progression of mathematical	incomplete progression of	Response includes an incom-	mathematical reasoning and	
understanding.	reasoning and understanding.	mathematical reasoning and	plete or illogical progression of	understanding.	
		understanding.	mathematical reasoning and		
		Contains minor errors .	understanding.		
5 points	4 points	3 points	2 points	1 point	

DATA DRIVEN INSTRUCTION

Formative assessments inform instructional decisions. Taking inventories and assessments, observing reading and writing behaviors, studying work samples and listening to student talk are essential components of gathering data. When we take notes, ask questions in a student conference, lean in while a student is working or utilize a more formal assessment we are gathering data. Learning how to take the data and record it in a meaningful way is the beginning of the cycle.

Analysis of the data is an important step in the process. What is this data telling us? We must look for patterns, as well as compare the notes we have taken with work samples and other assessments. We need to decide what are the strengths and needs of individuals, small groups of students and the entire class. Sometimes it helps to work with others at your grade level to analyze the data.

Once we have analyzed our data and created our findings, it is time to make informed instructional decisions. These decisions are guided by the following questions:

- What mathematical practice(s) and strategies will I utilize to teach to these needs?
- What sort of grouping will allow for the best opportunity for the students to learn what it is I see as a need?
- Will I teach these strategies to the whole class, in a small guided group or in an individual conference?
- Which method and grouping will be the most effective and efficient? What specific objective(s) will I be teaching?

Answering these questions will help inform instructional decisions and will influence lesson planning.

Then we create our instructional plan for the unit/month/week/day and specific lessons.

It's important now to reflect on what you have taught.

Did you observe evidence of student learning through your checks for understanding, and through direct application in student work?

What did you hear and see students doing in their reading and writing?



Now it is time to begin the analysis again.

Data Analysis Form	School:	Teacher:	Date:
Assessment:		NJSLS:	

GROUPS (STUDENT INITIALS)	SUPPORT PLAN	PROGRESS
MASTERED (86% - 100%) (PLD		
4/5):		
-7-)		
DEVELOPING (67% - 85%) (PLD		
3):		
5).		
INSECURE (51%-65%) (PLD 2):		
BEGINNING (0%-50%) (PLD 1):		

MATH PORTFOLIO EXPECTATIONS

The Student Assessment Portfolios for Mathematics are used as a means of documenting and evaluating students' academic growth and development over time and in relation to the CCSS-M. The September task entry(-ies) should reflect the prior year content and *can serve* as an additional baseline measure.

All tasks contained within the **Student Assessment Portfolios** should be aligned to NJSLS and be "practice forward" (closely aligned to the Standards for Mathematical Practice).

Four (4) or more additional tasks will be included in the **Student Assessment Portfolios** for Student Reflection and will be labeled as such.

K-2 GENERAL PORTFOLIO EXPECTATIONS:

- Tasks contained within the Student Assessment Portfolios are "practice forward" and denoted as "Individual", "Partner/Group", and "Individual w/Opportunity for Student Interviews¹.
- Each Student Assessment Portfolio should contain a "Task Log" that documents all tasks, standards, and rubric scores aligned to the performance level descriptors (PLDs).
- Student work should be attached to a completed rubric; with appropriate teacher feedback on student work.
- Students will have multiple opportunities to revisit certain standards. Teachers will capture each additional opportunity "as a new and separate score" in the task log.
- A 2-pocket folder for each Student Assessment Portfolio is *recommended*.
- All Student Assessment Portfolio entries should be scored and recorded as an Authentic Assessment grade (25%)².
- All Student Assessment Portfolios must be clearly labeled, maintained for all students, inclusive of constructive teacher and student feedback and accessible for review.

GRADES K-2

Student Portfolio Review

Provide students the opportunity to review and evaluate their portfolio at various points throughout the year; celebrating their progress and possibly setting goals for future growth. During this process, students <u>should retain ALL of their current artifacts</u> in their Mathematics Portfolio.

Resources

Number Book Assessment Link: http://investigations.terc.edu/

Model Curriculum- http://www.nj.gov/education/modelcurriculum/

Georgia Department of Education: Games to be played at centers with a partner or small group. <u>http://ccgpsmathematicsk-5.wikispaces.com/Kindergarten</u>

Engage NY: *For additional resources to be used during centers or homework. <u>https://www.engageny.org/sites/default/files/resource/attachments/math-gk-m1-full-module.pdf</u>

Add/ Subtract Situation Types: Darker Shading indicates Kindergarten expectations https://achievethecore.org/content/upload/Add%20Subtract%20Situation%20Types.pdf

Math in Focus PD Videos: <u>https://www-</u> <u>k6.thinkcentral.com/content/hsp/math/hspmath/common/mif_pd_vid/9780547760346_te/index.</u> <u>html</u>

Number Talk/string videos <u>https://hcpss.instructure.com/courses/124/pages/routines:</u>

Suggested Literature

Fish Eyes by, Lois Ehlert Ten Little Puppies by, Elena Vazquez Zin! Zin! A Violin! by, Lloyd Moss My Granny Went to the Market by, Stella Blackstone and Christopher Corr Anno's Couting Book by, Mitsumasa Anno Chicka, Chicka, 1,2,3 by, Bill Martin Jr.; Michael Sampson; Lois Ehlert How Dinosaurs Count to 10 by Jane Yolen and Mark Teague 10 Little Rubber Ducks by Eric Carle Ten Black Dots by Donald Crews Mouse Count by Ellen Stoll Walsh Count! by Denise Fleming

21st Century Career Ready Practices

CRP1. Act as a responsible and contributing citizen and employee.

CRP2. Apply appropriate academic and technical skills.

CRP3. Attend to personal health and financial well-being.

CRP4. Communicate clearly and effectively and with reason.

CRP5. Consider the environmental, social and economic impacts of decisions.

CRP6. Demonstrate creativity and innovation.

CRP7. Employ valid and reliable research strategies.

CRP8. Utilize critical thinking to make sense of problems and persevere in solving them.

CRP9. Model integrity, ethical leadership and effective management.

CRP10. Plan education and career paths aligned to personal goals.

CRP11. Use technology to enhance productivity.

CRP12. Work productively in teams while using cultural global competence.

For additional details see **<u>21st</u>** Century Career Ready Practices .

References

"Eureka Math" Great Minds. 2018 < https://greatminds.org/account/products>